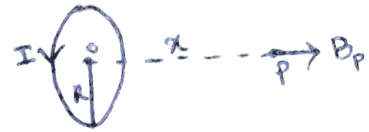


Sol : We are asked to calculate the Magnetic Field at center of current carrying loop.



So, Formula for that is,

$$B_{\text{centre}} = \frac{\mu_0 N I}{2R}$$

$N = \text{no. of loop}$

$\therefore$ There is only a single loop

$N = 1$

$I = \text{current in the loop}$

$R = \text{radius of the loop.}$

We Donot know the value of I

So, we find I value using the following :-

Given ,

magnetic field at the point 'p', 7cm away from

$$\text{centre}(B_p) = 48 \text{ MT} = 48 \times 10^6 \text{ T}$$

Using the formula,

magnetic field at a point 'p' on axis of the loop,

$$B_p = \frac{\mu_0 N I R^2}{2(R^2 + x^2)^{3/2}}$$

Given

$$B_p = 48 \times 10^6 \text{ T}$$

$$x = 7 \text{ cm} = 0.07 \text{ m}$$

$$R = 4 \text{ cm} = 0.04 \text{ m}$$

Given,

No. of loop $N = 1$

$$R = 4 \text{ cm} = 4 \times 10^{-2} \text{ m}$$

$$x = 7 \text{ cm} = 7 \times 10^{-2} \text{ m}$$

$$B_p = 48 \times 10^6 \text{ T}$$

$$48 \times 10^6 = \frac{\mu_0 I R^2}{2(x^2 + R^2)^{3/2}}$$

As we need 'I' value, we will rearrange the above formula,

$$I = \frac{48 \times 10^6 \times 2(x^2 + R^2)^{3/2}}{\mu_0 R^2}$$

$$I = \frac{96 \times 10^6 (x^2 + R^2)^{3/2}}{\mu_0 R^2}$$

②

Substitute eq. ② in eq. ①

$$B_{\text{centre}} = \frac{\cancel{\mu_0} \times \left[\frac{48}{\cancel{96}} \times 10^6 (x^2 + R^2)^{3/2} \right]}{\cancel{2} R \cancel{\mu_0} R^2}$$

$$= \frac{48 \times 10^6 (x^2 + R^2)^{3/2}}{R^3}$$

$$= 48 \times 10^6 \frac{\left((2 \times 10^{-2})^2 + (4 \times 10^{-2})^2 \right)^{3/2}}{(4 \times 10^{-2})^3}$$

$$= 48 \times 10^6 \frac{\left[(49 \times 10^{-4}) + (16 \times 10^{-4}) \right]^{3/2}}{64 \times 10^{-6}}$$

$$= \frac{48}{64} \times 10^6 \times 10^6 \times \left[10^{-4} (49 + 16) \right]^{3/2}$$

$$= \frac{3}{4} \times 10^{12} \left[10^{-4} \times 65 \right]^{3/2}$$

$$= \frac{3}{4} \times 10^{12} \left[(10^{-4} \times 65)^3 \right]^{1/2}$$

$$\because a^{m/n} = (a^m)^{1/n}$$

$$= \frac{3}{4} \times 10^{12} \left[10^{-12} \times 274625 \right]^{1/2}$$

$$= \frac{3}{4} \times 10^{12} \left[10^{-6} \times 524.04 \right]$$

$$= 393.03 \times 10^6 \text{ T}$$

$$B_{\text{centre}} = 393.03 \text{ MT}$$