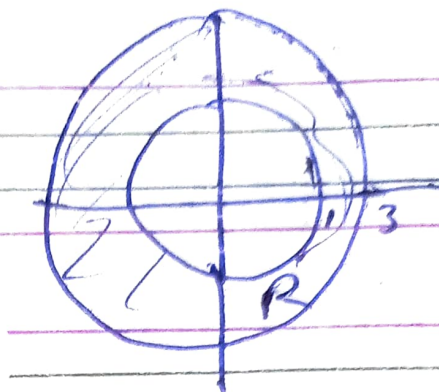


$$\vec{F} = (2x - y^3)\hat{i} - (xy)\hat{j}$$

since region is closed

use green's theorem



$$\int_C \vec{F} \cdot d\vec{r} = \iint_R \left(\frac{\partial N}{\partial x} - \frac{\partial M}{\partial y} \right) dx dy$$

$$= \iint_R (-y + 3y^2) dx dy$$

convert into polar

$$\int_{\theta=0}^{2\pi} \int_{r=1}^3 (-r \sin \theta + 3r^2 \sin^2 \theta) r dr d\theta$$

$$\int_{\theta=0}^{2\pi} \left[-\frac{r^2}{2} \sin \theta + \frac{3}{4} r^4 \sin^2 \theta \right]_{r=1}^3 d\theta$$

$$\Rightarrow \int_{\theta=0}^{2\pi} \left(-9 \sin \theta + \frac{3^5}{4} \sin^2 \theta - \left[-\frac{1}{2} \sin \theta + \frac{3}{4} \sin^2 \theta \right] \right) d\theta$$

$$\Rightarrow \int_{\theta=0}^{2\pi} \left(\frac{3^5}{4} \left(\frac{1 - \cos 2\theta}{2} \right) - \frac{3}{4} \left(\frac{1 - \cos 2\theta}{2} \right) \right) d\theta$$

$$2\pi \int_{\theta=0}^{\theta=2\pi} \frac{3^5}{8} - \frac{3^5 \cos 2\theta}{8} - \frac{3}{8} + \frac{3 \cos 2\theta}{8} d\theta$$

$$2\pi \times \left(\frac{3^5}{8} - 3 \right) = \frac{2\pi}{8} (240) = \boxed{60\pi} \text{ L}$$