

$$\nabla \times F = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ zx & xy & yz \end{vmatrix}$$

$$\hat{i}(z-0) + \hat{j}(0-x) + \hat{k}(y-0)$$

$$= z\hat{i} + x\hat{j} + y\hat{k}$$

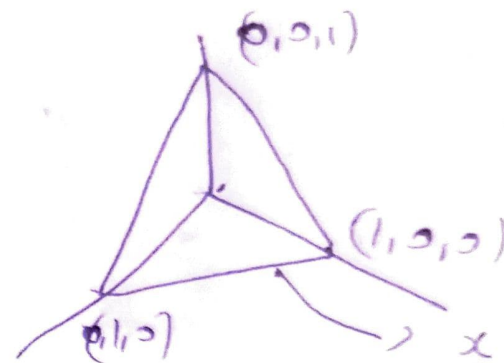
Since curve is closed, use Stokes theorem.

$$\int F \cdot d\mathbf{r} = \iint (\nabla \times F) \cdot \hat{n} \, dS = \iint \frac{x+y+z}{\sqrt{3}} \times \frac{dx \, dy}{\frac{1}{\sqrt{3}}}$$

$$= \iint (x+y+(1-x-y)) \, dx \, dy \Rightarrow \iint_A dx \, dy$$

$$= \int_{x=0}^1 \int_{y=0}^{1-x} dy \, dx = \int_{x=0}^1 (1-x) \, dx$$

$$\Rightarrow \left[x - \frac{x^2}{2} \right]_0^1 = 1 - \frac{1}{2} = \boxed{\frac{1}{2}}$$



$$\frac{x}{1} + \frac{y}{1} + \frac{z}{1} = 1$$

$$\hat{n} = \frac{\hat{i} + \hat{j} + \hat{k}}{\sqrt{3}}$$

