

option (a) $f: [a,b] \rightarrow (a,b) \rightarrow \text{cont. \& 1-1}$

let $\boxed{f(x) = \frac{x}{2}}$ then $f[a,b] = [\frac{a}{2}, \frac{b}{2}] \rightarrow \underline{\text{exist}}$

option (b)

$f: [a,b] \rightarrow (a,b) \rightarrow \text{cont. \& onto}$

$$\Rightarrow f[a,b] = (a,b)$$

$$\Rightarrow f^{-1}(a,b) = [a,b] \quad [\text{not onto}]$$

it's contradiction because pre-image of open set is open under continuous map, so not exist ✗

option - c

$f: (a,b) \rightarrow [a,b]$ f is cont. \& 1-1

$$\text{let } f(x) = x$$

$$f(a,b) = (a,b) \quad \text{\& 1-1 also}$$

so exist.

option (d)

$f: (a,b) \rightarrow [a,b]$, cont. \& onto

$$\Rightarrow f^{-1}[a,b] = (a,b) \quad [\text{not onto}]$$

it is again contradiction as
preimage of closed set should be closed
under continuous map. so not exist ✗