

let $\{a_n\}$ be bounded sequence.

let $a_n = \frac{1}{n}$ which is bounded between 0 & 1

$$0 < \frac{1}{n} \leq 1$$

define $x_n = \sup \{a_k : k > n\}$

$$x_1 = \sup \left\{ \frac{1}{k} : k > 1 \right\} = \frac{1}{2}$$

$$x_2 = \sup \left\{ \frac{1}{k} : k > 2 \right\} = \frac{1}{3}$$

$\vdots$

$$x_n = \frac{1}{n}$$

$$\Rightarrow x_1 > x_2 > x_3 > \dots > x_n$$

↓
decreasing sequence and bounded above

option ~~(A)~~, ~~(B)~~ and ~~(C)~~ are discarded.

option (D) is correct

proof :- since a_n is bounded sequence

$\Rightarrow \exists m \in \mathbb{R}$ such that

$$|a_n| \leq m$$

$$\Rightarrow -m \leq a_n \leq m \quad \forall n \in \mathbb{N}$$

$$x_n = m$$

$\Rightarrow$

$$\lim_{n \rightarrow \infty} x_n = m$$

Thus option (D) is correct