

Since we have to integrate in circle $x^2 + y^2 = a^2$
 we can convert into polar coordinates

$$\int_{-a}^a \int_{-\sqrt{a^2-x^2}}^{\sqrt{a^2-x^2}} \frac{a^2 - 3(a^2 - x^2 - y^2)}{\sqrt{a^2 - x^2 - y^2}} dx dy$$

$$\Rightarrow \int_0^{2\pi} \int_0^a \frac{a^2 - 3(a^2 - r^2)}{\sqrt{a^2 - r^2}} \times r dr d\theta$$

$$\Rightarrow \int_0^{2\pi} \int_0^a \frac{a^2 r}{\sqrt{a^2 - r^2}} - \int_0^{2\pi} \int_0^a 3\sqrt{a^2 - r^2} \times r dr d\theta$$

you can calculate yourself

$$\Rightarrow \frac{2\pi \times a^2 \times 2 \times \left[(a^2 - r^2)^{1/2} \right]_0^a}{-2} - \frac{2\pi \times 3 \times 2 \times \left[(a^2 - r^2)^{3/2} \right]_0^a}{-2 \times 3}$$

~~$$2\pi a^2 [\sqrt{1+a^2} - 1] + 2\pi [0 - a^3]$$~~

$$\Rightarrow -2\pi a^2 [0 - a] + 2\pi [0 - a^3]$$

$$\Rightarrow 2\pi a^3 - 2\pi a^3 = 0$$