

(A) :- In the question it is given that,

optical rotation of D-Galactose is $+70.7^\circ$

→ optical rotation of α -form of D-Galactose is $+125.7^\circ$

→ optical rotation of β -form of D-Galactose is $+50.8^\circ$

→ So,

we have to calculate the proportion of these α and β forms of D-Galactose in an equilibrium mixture.

→ It was given in the question that,

- Specific rotation of pure α -D-Galactose is $+125.7^\circ$

- Specific rotation of pure β -D-Galactose is $+50.8^\circ$

In an equilibrium mixture,

$$\text{Specific rotation of mixture} = \left[(\text{proportion of } \alpha\text{-form}) \times \text{Specific rotation of } \alpha\text{-form} \right] + \left[(\text{proportion of } \beta\text{-form}) \times \text{Specific rotation of } \beta\text{-form} \right]$$

$\downarrow$

$+70.7^\circ$ (Given)

Let's consider,

' x ' as the proportion of α -D-Galactose and $(1-x)$ is proportion of β -D-Galactose in equilibrium mixture.

So,

$$+70.7^\circ = [x \times 125.7] + [(1-x) \times 50.8] \quad (\text{Given in question})$$

$$70.7 = 125.7x + 50.8 - 50.8x$$

$$\begin{aligned} 70.7 - 50.8 &= 125.7x - 50.8x \\ 19.9 &= 74.9x \end{aligned}$$

$$x = \frac{19.9}{74.9}$$

$$x \approx 0.26$$

→ so, as we assumed proportion of α -D-Galactose = x
 ≈ 0.26

and,
 proportion of β -D-Galactose is $1-x = 1-0.26$
 ≈ 0.74

∴ In an equilibrium mixture of D-Galactose,

the proportion of α -D-Galactose is ≈ 0.26 and
 the proportion of β -D-Galactose is ≈ 0.74 .