YOUR INPUT: f(x) =

$$x^2 e^{-x^2}$$



Simplify

"MANUALLY" COMPUTED ANTIDERIVATIVE:

$$\int f(x) \, \mathrm{d}x = F^\star(x) =$$

"Manual" integration with steps:

The calculator finds an antiderivative in a comprehensible way. Note that due to some simplifications, it might only be valid for parts of the function.

$$rac{\sqrt{\pi}\operatorname{erf}(x)-2x\mathrm{e}^{-x^2}}{4}+C$$



Hide steps

Problem:

$$\int \! x^2 \mathrm{e}^{-x^2} \, \mathrm{d}x$$

Integrate by parts: $\int fg' = fg - \int f'g$

$$f = x$$
, $g' = xe^{-x^2}$
 $\downarrow \underline{\text{steps}}$ $\downarrow \underline{\text{steps}}$

$$f' = 1$$
, $g = -\frac{e^{-x^2}}{2}$:

$$=-rac{x{
m e}^{-x^2}}{2}-\int-rac{{
m e}^{-x^2}}{2}\,{
m d}x$$

Now solving:

$$\int -\frac{\mathrm{e}^{-x^2}}{2}\,\mathrm{d}x$$

Apply linearity:

$$= -\frac{\sqrt{\pi}}{4} \int \frac{2e^{-x^2}}{\sqrt{\pi}} \, \mathrm{d}x$$

Now solving:

$$\int \frac{2e^{-x^2}}{\sqrt{\pi}} \, \mathrm{d}x$$

This is a special integral (Gauss error function):

$$= \operatorname{erf}(x)$$

Plug in solved integrals:

$$-\frac{\sqrt{\pi}}{4} \int \frac{2e^{-x^2}}{\sqrt{\pi}} dx$$
$$= -\frac{\sqrt{\pi} \operatorname{erf}(x)}{4}$$

Plug in solved integrals:

$$-rac{x \mathrm{e}^{-x^2}}{2} - \int -rac{\mathrm{e}^{-x^2}}{2}\,\mathrm{d}x \ = rac{\sqrt{\pi} \operatorname{erf}(x)}{4} - rac{x \mathrm{e}^{-x^2}}{2}$$

Plug in solved integrals:

$$-rac{x\mathrm{e}^{-x^2}}{2} - \int -rac{\mathrm{e}^{-x^2}}{2}\,\mathrm{d}x \ = rac{\sqrt{\pi}\,\mathrm{erf}(x)}{4} - rac{x\mathrm{e}^{-x^2}}{2}$$

The problem is solved:

$$\int \! x^2 \mathrm{e}^{-x^2} \, \mathrm{d}x$$
 $= rac{\sqrt{\pi} \operatorname{erf}(x)}{4} - rac{x \mathrm{e}^{-x^2}}{2} + C$ Rewrite/simplify: $= rac{\sqrt{\pi} \operatorname{erf}(x) - 2x \mathrm{e}^{-x^2}}{4} + C$

ANTIDERIVATIVE COMPUTED BY MAXIMA:

$$\int f(x) \, \mathrm{d}x = F(x) =$$

$$\frac{\sqrt{\pi}\operatorname{erf}(x)}{4} - \frac{x\mathrm{e}^{-x^2}}{2} + C$$



Simplify

DEFINITE INTEGRAL:

$$\int\limits_0^\infty f(x)\,\mathrm{d}x =$$

$$\frac{\sqrt{\pi}}{4}$$

