

formula - $\sin x - \sin y = 2 \cos \left(\frac{x+y}{2} \right) \cdot \sin \left(\frac{x-y}{2} \right)$

(b) $|\sin 2x - \sin 2y| = |2 \cos(x+y) \cdot \sin(x-y)|$

$$\leq |2| |\cos(x+y)| |\sin(x-y)|$$

$$= |x-y|$$

option (b) ✓

(a) $|\sin^2 x - \sin^2 y| = |(\sin^2 x + \sin^2 y)(\sin x - \sin y)|$

$$\leq \underbrace{|\sin x + \sin y|}_{\text{bounded}} |\sin x - \sin y|$$

$$\leq K \left| \frac{x-y}{2} \right| \quad [\text{from option (b)}]$$

$$= c|x-y| < |x-y|$$

option (a) ✓

(c) since $e^x > x \quad \forall x \in \mathbb{R}$

$$\Rightarrow |e^x - e^y| \geq |x-y| \quad \text{option (c) ✓}$$

(d) $e^x \cos x + 1 = 0$

$x = \pi, 3\pi, \dots, (2n-1)\pi$ are roots

option (d) X

$|\cos x| \leq 1 \quad \forall x, \forall \mathbb{R}$

$|\sin x| \leq x$