

$$x_0 = 4 \quad ; \quad x_{n+1} = \sqrt{x_n}$$

$$n=0 \quad x_1 = \sqrt{x_0} = \sqrt{4} = 2$$

$$n=1 \quad x_2 = \sqrt{x_1} = \sqrt{2} = (2)^{1/2}$$

$$n=2 \quad x_3 = \sqrt{x_2} = \sqrt{\sqrt{2}} = (2)^{1/2^2}$$

$$n=3 \quad ; \quad x_4 = \sqrt{x_3} = \sqrt{\sqrt{\sqrt{2}}} = (2)^{1/2^3}$$

1

4

$$y_n = 2^n (x_n - 1) \quad \forall n \in \mathbb{N}$$

$$y_1 = 2^1 (x_1 - 1) = 2(2 - 1) = 2$$

$$y_2 = 2^2 (x_2 - 1) = 2^2 (\sqrt{2} - 1) = 2^2 (2^{1/2} - 1)$$

$$y_3 = 2^3 (x_3 - 1) = 2^3 ((2)^{1/2^2} - 1)$$

$$y_4 = 2^4 (x_4 - 1) = 2^4 ((2)^{1/2^3} - 1)$$

1

$$y_K = 2^K (x_K - 1) = 2^K \left((2)^{\frac{1}{2^{K-1}}} - 1 \right)$$

monotonically
increasing

decreasing bounded

1

$$\lim_{n \rightarrow \infty} y_n = \lim_{n \rightarrow \infty} 2^n \left[(2)^{\frac{1}{2^{n-1}}} - 1 \right]$$

$$\underline{\underline{= 0}}$$