

① A function $f(x, y)$ is called homogeneous if $f(tx, ty) = t^\alpha f(x, y)$ of degree α .

Now here given

$$f(x, y) = x + y^2$$

$$f(tx, ty) = tx + t^2 y^2 = t(x + ty^2) \neq t^\alpha f(x, y)$$

So, not homogeneous

hence, not homogeneous.

option (B), (D) are correct

③ $u'(t) = 4u^{3/4}(t) \quad u(0) = 0$

$$\int \frac{du}{u^{3/4}} = \int 4 dt$$

$$4(u)^{1/4} = 4t + C$$

$$= u = (t + C)^4 \quad \text{--- } \textcircled{\star}$$

$u(0) = 0$ gives

$$\boxed{u(t) = t^4}$$

$\Rightarrow u(t) = 0$ is also trivial solution.

$\Rightarrow$ from $\textcircled{\star}$, by shifting curve $u(t) = t^4$ on x-axis

$$u(t) = \begin{cases} 0 & 0 < t < \pi \\ (t - \pi)^4 & t \geq \pi \end{cases}$$

put $\pi = 1$ and so then C, D are correct

So, option A, B, C, D are correct