

$$1 - \frac{1}{3!} + \frac{1}{5!} - \frac{1}{7!} + \dots - \frac{1}{(2n-1)!}$$

$$\Rightarrow \sum (-1)^n \cdot \frac{1}{(2n-1)!} = \sum (-1)^n \cdot b_n$$

where  $b_n = \frac{1}{(2n-1)!}$

$$\lim_{n \rightarrow \infty} b_n = \lim_{n \rightarrow \infty} \frac{1}{(2n-1)!} = \frac{1}{\infty} = 0$$

$$\lim_{n \rightarrow \infty} b_n = 0$$

$$b_n = \frac{1}{(2n-1)!} ; \quad b_{n+1} = \frac{1}{(2n+1)!}$$

$$\therefore (2n+1)! > (2n-1)! \quad \forall n \in \mathbb{N}$$

$$\Rightarrow \frac{1}{(2n+1)!} < \frac{1}{(2n-1)!}$$

$$\Rightarrow \frac{1}{(2n+1)!} - \frac{1}{(2n-1)!} < 0$$

$$\Rightarrow b_{n+1} - b_n < 0$$

$$\Rightarrow \underline{b_{n+1} < b_n} \Rightarrow \{b_n\} \text{ is monotonic}$$

decreasing sequence so it satisfies both conditions of alternating series (Leibnitz test)

$\Rightarrow$  Series is convergent