

$$s_k = \sum_{k=1}^n a_k$$

now $s_2 - s_1 = a_2 + a_1 - a_1 = a_2$

$$s_1 = a_1$$

$$s_2 = a_1 + a_2$$

$$s_3 = a_1 + a_2 + a_3$$

$$s_4 = a_1 + a_2 + a_3 + a_4$$

$$a_2 = s_2 - s_1$$

similarly

$$a_3 = s_3 - s_2$$

$$a_4 = s_4 - s_3$$

$$a_n = s_n - s_{n-1}$$

now $t_n = \sum_{k=2}^n \frac{a_k}{s_{k-1} s_k}$

$$t_n = \frac{a_2}{s_1 s_2} + \frac{a_3}{s_2 s_3} + \frac{a_4}{s_3 s_4} + \dots + \frac{a_n}{s_{n-1} s_n}$$

$$= \left(\frac{s_2 - s_1}{s_1 s_2} \right) + \left(\frac{s_3 - s_2}{s_2 s_3} \right) + \left(\frac{s_4 - s_3}{s_3 s_4} \right) + \dots + \left(\frac{s_n - s_{n-1}}{s_{n-1} s_n} \right)$$

$$s_n = \sum_{k=1}^n a_k =$$

$$t_n = \sum_{k=2}^n \frac{a_k}{s_k - s_{k-1}}$$

$$= \frac{a_2}{s_1 s_2} + \frac{a_3}{s_2 s_3} + \frac{a_4}{s_3 s_4} + \frac{a_5}{s_4 s_5} + \dots + \frac{a_n}{s_{n-1} s_n}$$

$$= \left(\frac{1}{s_1} - \frac{1}{s_2} \right) a_2 + \left(\frac{1}{s_2} - \frac{1}{s_3} \right) a_3 + \left(\frac{1}{s_3} - \frac{1}{s_4} \right) a_4 + \dots + \left(\frac{1}{s_{n-1}} - \frac{1}{s_n} \right) a_n$$

$$= \left(\frac{s_2 - s_1}{s_1 s_2} \right) a_2 + \left(\frac{s_3 - s_2}{s_2 s_3} \right) a_3 + \left(\frac{s_4 - s_3}{s_3 s_4} \right) a_4 + \dots$$

$$t_n = \left(\frac{1}{s_1} - \frac{1}{s_2} \right) + \left(\frac{1}{s_2} - \frac{1}{s_3} \right) + \left(\frac{1}{s_3} - \frac{1}{s_4} \right) + \dots + \left(\frac{1}{s_{n-1}} - \frac{1}{s_n} \right)$$

$$= \frac{1}{s_1} - \frac{1}{s_n}$$

∵ $\sum t_n$ is divergent
then $s_n = \sum a_k$ is also divergent

∴
 $\lim_{n \rightarrow \infty}$

$$t_n = \lim_{n \rightarrow \infty} \left(\frac{1}{s_1} - \frac{1}{s_n} \right)$$

$$\lim_{n \rightarrow \infty} \frac{1}{s_n} = \frac{1}{\infty} = 0$$

$$= \frac{1}{s_1} - 0$$

$$= \frac{1}{a_1}$$