

P.O.T.

$$\frac{1}{(D'+1)^2} \cdot \frac{1}{(1-e^z)^2} = \frac{1}{(D'+1)} \cdot \left\{ \frac{1}{(D'+1)} \cdot \frac{1}{(1-e^z)^2} \right\}$$

$$= \frac{1}{(D'+1)} \left\{ \frac{1 \cdot Q(z)}{(D'+1)} \right\} \quad \text{where} \quad Q(z) = \frac{1}{(1-e^z)^2}$$

$$= \frac{1}{(D'+1)} \left[e^{-z} \int e^z \cdot Q(z) dz \right]$$

$$= \frac{1}{(D'+1)} \left[e^{-z} \int e^z \cdot \frac{1}{(1-e^z)^2} dz \right]$$

$$\text{put } 1-e^z = t$$

$$e^z dz = -dt$$

$$\left(\frac{1}{D'+1}\right) \left[e^{-z} \int \frac{-dt}{t^2} \right]$$

$$= \left(\frac{1}{D'+1}\right) \left[e^{-z} \left(\frac{1}{t} \right) \right]$$

$$= \frac{1}{(D'+1)} \left(\frac{e^{-z}}{1-e^z} \right) = \frac{1}{(D'+1)} (Q'(z)) \quad \text{where} \quad Q'(z) = \frac{e^{-z}}{1-e^z}$$

$$= e^{-z} \int e^z \cdot Q'(z) dz$$

$$= e^{-z} \int e^z \frac{e^{-z}}{1-e^z} dz$$

$$= e^{-z} \int \frac{1}{1-e^z} dz$$

$$= e^{-z} \int \left(1 - \frac{e^z}{1-e^z} \right) dz$$

$$= e^{-z} (z - \log(e^z - 1))$$

$$\therefore z = \log x$$

$$= e^{-\log x} [\log x - \log(e^{\log x} - 1)]$$

$$= \frac{1}{x} [\log x - \log(x-1)]$$
