

$$\text{let } F = (x^2 - y^2 + x)\hat{i} + (-y)(2xy + y)\hat{j}$$

$$\nabla \times F = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ x^2 - y^2 + x & -2xy - y & 0 \end{vmatrix} = \hat{i}(0) - \hat{j}(0) + \hat{k}(-2y + 2y) = \vec{0}$$

$\Rightarrow F$ is irrotational

let ϕ be scalar potential

then $\frac{\partial \phi}{\partial x} = x^2 - y^2 + x$

$$\Delta \quad \frac{\partial \phi}{\partial y} = -2xy - y$$

$$\phi = \frac{x^3}{3} - \frac{y^2 x}{2} + \frac{x^2}{2}$$

$$\Delta \quad \phi = -xy^2 - \frac{y^2}{2}$$

Then $\boxed{\phi = \frac{x^3}{3} - y^2 x + \frac{x^2}{2} - xy^2 - \frac{y^2}{2}}$