

Identity element in $(\mathbb{Z}_5, \times_5)$ over 2×2 non singular matrix is $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$.

Inverse of A must satisfy $A \otimes_5 B = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

checking By options

a).

$$B = \begin{bmatrix} 3 & -3 \\ 0 & 2 \end{bmatrix}$$

$$A = \begin{bmatrix} 2 & 3 \\ 2 & 4 \end{bmatrix}$$

$$A \otimes_5 B = \begin{bmatrix} 1 & 0 \\ 1 & 2 \end{bmatrix} \neq I$$

b).

$$B = \begin{bmatrix} 2 & 1 \\ 4 & 1 \end{bmatrix}, \quad A \otimes_5 B = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = I$$

c).

$$B = \begin{bmatrix} 3 & 5 \\ 5 & 4 \end{bmatrix}, \quad A \otimes_5 B = \begin{bmatrix} 1 & 2 \\ 1 & 1 \end{bmatrix} \neq I$$

d).

$$B = \begin{bmatrix} 3 & 2 \\ 3 & 4 \end{bmatrix}, \quad A \otimes_5 B = \begin{bmatrix} 0 & 1 \\ 3 & 0 \end{bmatrix} \neq I$$

option a), c), d) are correct.