

$$f(x) = \begin{cases} -1, & \frac{1}{2} \leq x < 1 \\ 1, & \frac{1}{3} \leq x < \frac{1}{2} \\ -1, & \frac{1}{4} \leq x < \frac{1}{3} \\ 1, & \frac{1}{5} \leq x < \frac{1}{4} \\ -1, & \frac{1}{6} \leq x < \frac{1}{5} \\ \vdots & \end{cases} \quad \begin{cases} 0, & x=0 \\ 1, & x=1 \end{cases}$$

at $x=1$ $f(1) = 1$, $L.H.L. = \lim_{x \rightarrow 1^-} f(x) = -1$
 $L.H.L. \neq f(1)$ f is discontinuous at $x=1$.

at $x = \frac{1}{2}$, $f(\frac{1}{2}) = -1$
 $L.H.L. \quad \lim_{x \rightarrow \frac{1}{2}^-} f(x) = 1$
 $R.H.L. \quad \lim_{x \rightarrow \frac{1}{2}^+} f(x) = -1$

$L.H.L. \neq R.H.L.$ f is discts. at $x = \frac{1}{2}$

Similarly doing this f is discontinuous at each $x = \frac{1}{n}$, $n \in \mathbb{N}$.

f is discontinuous at $x = 1, \frac{1}{2}, \frac{1}{3}, \dots$