

$$(1+x+x^2+\dots)(x^2+x^4+\dots)(1+x^3+x^5)$$

$$\Rightarrow 1(x^0 \cdot x^{80} + x^2 \cdot x^{78} + x^4 \cdot x^{76} + \dots x^{78} \cdot x^2)$$

$$+ x^3(x \cdot x^{76} + x^3 \cdot x^{74} + x^5 \cdot x^{72} + \dots x^{75} \cdot x^2)$$

$$+ x^5(x \cdot x^{74} + x^3 \cdot x^{72} + x^5 \cdot x^{70} + \dots x^{73} \cdot x^2) - \star$$

$\Rightarrow$ Now to find no. of elements in

$$x^0 \cdot x^{80} + x^2 \cdot x^{78} + \dots x^{78} \cdot x^2$$

first term $a = 0$

Common difference $d = 2$

by A.P

$$\bullet 78 = 0 + (n-1)2$$

$$39 = n-1 \Rightarrow$$

$$\boxed{n = 40}$$

①

[See, power of x is increasing by 2.]

$\Rightarrow$ Now to find no. element in

$$x \cdot x^{76} + x^3 \cdot x^{74} + \dots x^{75} \cdot x^2$$

$$a = 1 \quad d = 2 \quad \text{last term} = 75$$

$$75 = 1 + (n-1)2 \Rightarrow \boxed{n = 38}$$

$\rightarrow$

$\Rightarrow$ Now to find no. of element in

$$x \cdot x^{74} + x^3 \cdot x^{72} + \dots x^{73} \cdot x^2$$

$$a = 1 \quad d = 2$$

$$\text{last term} = 73$$

$$73 = 1 + (n-1)2 \Rightarrow$$

$$\boxed{n = 37}$$

Then no. of elements in $\star = 40 + 38 + 37 = \boxed{115}$

Then coefficient of

$$x^{80} =$$

$$\boxed{115}$$

Ans.