

We know

$$\frac{\partial}{\partial}(u.v.w) = v.w.\frac{\partial}{\partial}(u) + u.v.\frac{\partial}{\partial}(w) + u.w.\frac{\partial}{\partial}(v)$$

(i)

eg let take

$$y = (x+1)(x+2)(x+3)$$

$$\frac{\partial y}{\partial x} = (x+2)(x+3) \frac{\partial}{\partial x}[(x+1)] + (x+1)(x+3) \frac{\partial}{\partial x}[(x+2)]$$

$$+ (x+1)(x+2) \frac{\partial}{\partial x}[(x+3)]$$

[using (i) result]

$$\Rightarrow \frac{\partial y}{\partial x} = (x+2)(x+3) + (x+1)(x+3) + (x+1)(x+2)$$

⇒ Similarly

$$\text{take } y = (x+1)(x+2) \dots (x+2020)$$

$$\text{then } \frac{\partial y}{\partial x} = (x+2)(x+3) \dots (x+2020) \frac{\partial}{\partial x}[(x+1)] + (x+1)(x+3) \dots (x+2020) \frac{\partial}{\partial x}[(x+2)]$$

+ ...

$$\frac{\partial y}{\partial x} = (x+1)(x+3) \dots (x+2020) + (x+1)(x+2) \dots (x+2020) + \dots + (x+1)(x+2) \dots (x+2019)$$