

$$x+y = cx^2 \quad \text{--- (1)} \quad \Rightarrow \quad \frac{x^2}{x^2} + \frac{y}{x^2} = c$$

and given that $\tan x = 2$

Now diff. eqn (1) with respect to 'x'

$$1 + \frac{dy}{dx} = 2cx$$

$$\frac{1}{x} + \frac{y}{x^2} = c$$

$$\frac{dy}{dx} =$$

$$-\frac{1}{x^2} + \frac{x^2 \frac{dy}{dx} - y \cdot 2x}{x^4} = 0$$

$$\frac{-x^2 + x^2 \frac{dy}{dx} - 2xy}{x^4} = 0$$

$$x^2 \frac{dy}{dx} - 2xy - x^2 = 0$$

$$x^2 \frac{dy}{dx} = 2xy + x^2$$

$$\frac{dy}{dx} = \frac{2xy + x^2}{x^2} = 1 + \frac{2y}{x}$$

$$\boxed{\frac{dy}{dx} = 1 + \frac{2y}{x}}$$

$$\boxed{P = \frac{dy}{dx} = 1 + \frac{2y}{x}} \quad \text{--- (2)}$$

in eqn (2) we replace p by $\frac{p + \tan x}{1 - p \tan x}$

$$\frac{p + \tan x}{1 - p \tan x} = 1 + \frac{2y}{x}$$

$$\frac{p + 2}{1 - 2p}$$

$$Px + 2x = (x+2y)(1-2P)$$

$$Px + 2x = x+2y - 2P(x+2y)$$

$$Px + 2x = x+2y - 2Px - 4Py$$

$$Px + 2Px + 4Py = x+2y - 2x$$

$$3Px + 4Py = 2y - x$$

$$P(3x+4y) = 2y - x$$

$$P = \frac{2y-x}{3x+4y} = \frac{2y-x}{4y+3x}$$

$$\frac{dy}{dx} = \frac{2y-x}{4y+3x} \quad \text{--- (3)}$$

Now we put $y=vx$

$$v \frac{dy}{dx} = v + x \frac{dv}{dx}$$

Put the value of $y, \frac{dy}{dx}$ in (3)

$$v + x \frac{dv}{dx} = \frac{2vx-x}{4vx+3x} = \frac{2v-1}{4v+3}$$

$$x \frac{dv}{dx} = \frac{2v-1}{4v+3} - v = \frac{2v-1-4v^2-3v}{4v+3}$$

$$x \frac{dv}{dx} = - \frac{(1+v+4v^2)}{4v+3}$$

$$\frac{(4v+3) dv}{4v^2+v+1} = - \frac{dx}{x}$$

$$\int \frac{4v+3}{4v^2+v+1} \cdot dv = -\int \frac{dx}{x}$$

$$\frac{1}{2} \ln |64v^2 + 16v + 16| + \sqrt{\frac{5}{3}} \tan^{-1} \left(\frac{1}{\sqrt{15}} (8v+1) \right) = -\log x + \log c$$

$$\frac{1}{2} \ln (64v^2 + 16v + 16) + \sqrt{\frac{5}{3}} \tan^{-1} \left(\frac{1}{\sqrt{15}} (8v+1) \right) = \log \frac{c}{x}$$

put value of 'v'

$$\frac{1}{2} \ln \left(64 \left(\frac{y}{x} \right)^2 + 16 \left(\frac{y}{x} \right) + 16 \right) + \sqrt{\frac{5}{3}} \tan^{-1} \left(\frac{1}{\sqrt{15}} \left(8 \frac{y}{x} + 1 \right) \right) = \log \frac{c}{x}$$

Hence above expression is family of oblique trajectory.